

# New York City Department of Education

## Mathematics Overview – Grade 6

### 2012-13 School Year

#### Overview

This document was created after closely examining the Common Core Learning Standards (CCLS) and the previous New York State Standards. It provides a high-level CCLS-aligned scope and sequence for Mathematics that also takes into account the differences in and transition from the New York State Standards. The scope and sequence is aligned to the Common Core and demonstrates a focus on the major work of the grade<sup>1</sup>, which the [State has indicated](#) will be the focus of next year’s 3-8 State exams. It is not based on any additional information about the changes in next year’s tests. This scope and sequence represents one way that a school may choose to organize and teach the full range of the standards before the state test. This document contains the following components:

- **Year-long Overview:** A one-page view of the year that shows the:
  - **Unit Summary:** The number of suggested units across the year and the amount of instructional time spent on each unit. The instructional time is represented as pre-State test and post-State test.
  - **Omitted Concepts:** Concepts that are no longer taught at this grade-level according to the CCLS.
  - **Omitted Lessons:** Lessons within existing curriculum resources that should no longer be taught within this grade level according to the Common Core Learning Standards.
  - **Bridge Guidance:** Concepts that would have been taught in earlier grades, according to the Common Core, but were not part of the New York State Standards. They should be considered and woven into units during transition years since the concepts were not previously addressed/addressed fully in the New York State Standards. We ask that you consider the needs of your students when deciding if it is necessary to teach these concepts.
- **High-level Unit Overviews:** Overviews of each unit that include the:
  - **Unit Description:** A narrative description of the concepts the unit is intended to cover and the amount of instructional time suggested.
  - **Standards:** The group of related standards that should be taught within the unit.
  - **Impact Lessons & Other Resources Available:** A sample of suggested instructional resources for each unit, highlighting corresponding activities from *Impact Math* and *Everyday Math* (for bridge guidance only), as well as freely-available supplemental materials from a variety of online sources. Supplemental materials are activities that address standards cited within the unit. Educators can consider integrating all of the resources listed, as well as their own supplemental resources, to support addressing all of the standards covered in the unit. Note: these resources are **not sequenced** and are listed by standard.

#### How to Use:

To use this document, teacher teams could:

- Review the year-long and unit overviews to assess whether the scope and sequence makes sense for their school.
- Review the resources available by standard in each high-level unit overview.
- Use the high-level unit overviews and resources available to teach a sequence of instruction that fully addresses the standards represented.

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<sup>1</sup> For a listing of content emphases by cluster, refer to <http://engageny.org/resource/math-content-emphases>. For additional guidance—including key advances by grade, opportunities for in-depth focus, connections between content and practice standards, etc.—refer to [http://www.parcconline.org/sites/parcc/files/PARCC%20MCP%20for%20Mathematics\\_Fall%202011%20Release.pdf](http://www.parcconline.org/sites/parcc/files/PARCC%20MCP%20for%20Mathematics_Fall%202011%20Release.pdf). With questions or feedback on this document, please email [commoncorefellows@schools.nyc.gov](mailto:commoncorefellows@schools.nyc.gov).

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### Grade 6 Year-Long Overview:

This table shows an overview of all units that should be taught across the year and the recommended instructional time for each unit<sup>1</sup>.

Grade 6: Suggested Distribution of Units in Instructional Days	Time	# of weeks
Unit 1: Multiplying & Dividing	12.5%	<b>4 Weeks</b>
Unit 2: Ratios	20%	<b>5 Weeks</b>
Unit 3: Introduction to Rational Numbers	15%	<b>4 Weeks</b>
Unit 4: Expressions	20%	<b>5 Weeks</b>
Unit 5: Equations	20%	<b>5 Weeks</b>
Unit 6: Concepts in Geometry	5%	<b>1 Week</b>
Unit 7: Introduction to Statistics	7.5%	<b>2 Weeks</b>
<b>State Test</b>		
Post-test: After the state test, teachers should consider focusing their instruction on re-visiting the <i>key advances from the previous grade</i> and the <i>grade level fluency expectations and/or culminating standards</i> identified in the PARCC Content Model Frameworks. Students should continue to solve a wide scope of problems corresponding to the <i>key advances from the previous grade</i> and receive sufficient support and opportunities for practice with the <i>grade level fluency expectations and/or culminating standards</i> .		

#### Omitted Concepts:

- Area of a sector
- Estimate volume, area, and circumference
- Identify customary and metric units
- Identify radius, diameter, chords, and central angle
- Understand relationship between radius and diameter
- Understand relationship between circumference and diameter
- Use Venn diagram to sort data
- Sampling
- Translate two-step equations
- Read and write whole numbers to trillions
- Probability of compound and dependent events
- Counting Principle to determine size of sample space
- Proportions
- Calculate lengths of sides of similar triangles

#### Omitted Lessons from Impact Math:

- 1.1, 1.2, 1.3
- 2.1, 2.2, 2.3
- 4.1
- 5.2, 5.3
- 10.3, 10.4

#### Bridge Concepts

- Use understanding of *equivalent* fractions as a strategy to add and subtract fractions, including fractions with unlike denominators.
- Apply their understanding of multiplication to multiply fractions with like and unlike denominators, including mixed numbers.
- Solve real world problems involving multiplication of fractions and mixed numbers.
- Interpret multiplication as scaling, and explain the product when multiplying a given number by a fraction greater than or less than 1.
- Understand concepts of volume and relate volume to multiplication and addition.
- Interpret division of a unit fraction by a non-zero whole number and vice versa.

<sup>1</sup> Unit overviews and suggested instructional time are based on the *Draft Curriculum Maps in Mathematics: Overview of Grades 5-8 Units* developed by Student Achievement Partners.

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### Unit 1: Multiplying and Dividing – (4 Weeks)

**DESCRIPTION:**

Using the meanings of fractions, multiplication and division, and the relationship between multiplication and division, students will understand and explain why the procedures for dividing fractions make sense. They will interpret and compute quotients of fractions and solve word problems involving division of fractions by fractions. These skills can be applied in solving volume problems where the edge lengths have fractional values. By the end of 6<sup>th</sup> grade, students are expected to fluently (with speed and accuracy) divide multidigit numbers and compute with multidigit decimals, using the standard algorithms. These skills should be solidified in this unit. The Mathematical Practices should be evident throughout instruction and connected to the content addressed in this unit. Students should engage in mathematical tasks that provide an opportunity to connect content and practices.

Standards	Impact Lessons & Other Resources Available	Pages
<p>The standards and resources listed below are <b>not</b> intentionally sequenced and should <b>not</b> be taught consecutively. To teach the concepts represented in this unit, teacher teams could use this unit overview and other available resources to craft a coherent and focused sequence of instruction that fully addresses the standards and description of this unit.</p>		
<p>6.NS.1 Interpret and compute quotients of fractions, and solve word problems involving division of fractions by fractions, e.g., by using visual fraction models and equations to represent the problem. For example, create a story context for <math>(2/3) \div (3/4)</math> and use a visual fraction model to show the quotient; use the relationship between multiplication and division to explain that <math>(2/3) \div (3/4) = 8/9</math> because <math>3/4</math> of <math>8/9</math> is <math>2/3</math>. (In general, <math>(a/b) \div (c/d) = ad/bc</math>.) How much chocolate will each person get if 3 people share <math>1/2</math> lb of chocolate equally? How many <math>3/4</math>-cup servings are in <math>2/3</math> of a cup of yogurt? How wide is a rectangular strip of land with length <math>3/4</math> mi and area <math>1/2</math> square mi?</p>	<p>Impact Lesson 4.2 – Add and Subtract Fractions</p>	<p>26-232, parts of 233-241</p>
<p>6.G.2 Find the volume of a right rectangular prism with fractional edge lengths by packing it with unit cubes of the appropriate unit fraction edge lengths, and show that the volume is the same as would be found by multiplying the edge lengths of the prism. Apply the formulas <math>V = lwh</math> and <math>V = bh</math> to find volumes of right rectangular prisms with fractional edge lengths in the context of solving real-world and mathematical problems.</p>	<p>Impact Lesson 7.3 – Surface Area and Volume</p>	<p>434-448</p>
	<p>Impact Lesson 7.4 – Capacity</p>	<p>451-453</p>
<p>6.NS.2 Fluently divide multi-digit numbers using the standard algorithm.</p>	<p><a href="http://www.illustrativemathematics.org/illustrations/270">www.illustrativemathematics.org/illustrations/270</a> (Interpreting a Division Computation) - <a href="http://www.illustrativemathematics.org/illustrations/271">http://www.illustrativemathematics.org/illustrations/271</a> (Incorrect Division) <a href="http://www.homeschoolmath.net/teaching/md/long_division_why.php">http://www.homeschoolmath.net/teaching/md/long_division_why.php</a> <a href="https://cca6summer2011.wikispaces.com/Tasks+by+Domain%2C+Cluster%2C+and+Stan">https://cca6summer2011.wikispaces.com/Tasks+by+Domain%2C+Cluster%2C+and+Stan</a></p>	

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	<u>dard</u>	
6.NS.3 Fluently add, subtract, multiply, and divide multi-digit decimals using the standard algorithm for each operation.	Impact Lesson 4.3 – Multiply and Divide Decimals	242-263
6.NS.4 Find the greatest common factor of two whole numbers less than or equal to 100 and the least common multiple of two whole numbers less than or equal to 12. Use the distributive property to express a sum of two whole numbers 1–100 with a common factor as a multiple of a sum of two whole numbers with no common factor. For example, express $36 + 8$ as $4(9 + 2)$ .	Impact Lesson 3.4 – Apply Properties	175-183

### Bridge Guidance:

Standards	Impact Lessons & Other Resources Available	Pages
5.NF.1 Add and subtract fractions with unlike denominators (including mixed numbers) by replacing given fractions with equivalent fractions in such a way as to produce an equivalent sum or difference of fractions with like denominators. For example, $\frac{2}{3} + \frac{5}{4} = \frac{8}{12} + \frac{15}{12} = \frac{23}{12}$ . (In general, $\frac{a}{b} + \frac{c}{d} = \frac{ad + bc}{bd}$ .)	EDM 6.8 – Using A Slide Rule To Add And Subtract Fractions	MJ1 (191-192); MM (174)
	EDM 6.9 – Clock Fractions And Common Denominators	MJ1 (196- 197); MM (178)
	EDM 6.10 – Quick Common Denominators	MJ1 (200-201); MM (181-182)
	EDM 8.2 – Adding Mixed Numbers	MJ2 ( 252); MM (223)
	EDM 8.3 – Subtracting Mixed Numbers	MM (224- 225); MM (488); MJ2 (255)
5.NF.4: Apply and extend previous understandings of multiplication to multiply a fraction or whole number by a fraction. a. Interpret the product $(\frac{a}{b}) \times q$ as a parts of a partition of $q$ into $b$ equal parts; equivalently, as the result of a sequence of operations $a \times q \div b$ . For example, use a visual fraction model to show $(\frac{2}{3}) \times 4 = \frac{8}{3}$ , and create a story context for this equation. Do the same with $(\frac{2}{3}) \times (\frac{4}{5}) = \frac{8}{15}$ . (In general, $(\frac{a}{b}) \times (\frac{c}{d}) = \frac{ac}{bd}$ .) b. Find the area of a rectangle with fractional side lengths by tiling it with unit squares of the appropriate unit fraction side lengths, and show that the area is the same as would be found by multiplying the side lengths. Multiply fractional side lengths to find areas of rectangles, and represent fraction products as rectangular areas.	EDM 8.5 – Fractions Of Fractions	MJ2 (259- 261), MM (229, 220)
	EDM 8.6 – An Area Model For Fraction Multiplication	MJ2 (264- 266), MM (232-234)
	EDM 8.7 – Multiplication of Fractions And Whole Numbers	MJ2 (269, 270), MM (235, 236)
5.NF.5: Interpret multiplication as scaling (resizing), by: a. Comparing the size of a product to the size of one factor on the basis of the size of the other factor, without performing the indicated multiplication. b. Explaining why multiplying a given number by a fraction greater than 1 results in a product greater than the	EDM 8.2 – Adding Mixed Numbers	MJ2 (224, 255), MM (250-252)

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<p>given number (recognizing multiplication by whole numbers greater than 1 as a familiar case); explaining why multiplying a given number by a fraction less than 1 results in a product smaller than the given number; and relating the principle of fraction equivalence <math>a/b = (n \times a)/(n \times b)</math> to the effect of multiplying <math>a/b</math> by 1.</p>		
<p>5.NF.6: Solve real world problems involving multiplication of fractions and mixed numbers, e.g., by using visual fraction models or equations to represent the problem.</p>	<p>EDM 8.8 – Multiplication Of Mixed Numbers</p>	<p>MJ2 (273, 274), MM (237)</p>
<p>5.NF.7 Apply and extend previous understandings of division to divide unit fractions by whole numbers and whole numbers by unit fractions.</p> <p>a. Interpret division of a unit fraction by a non-zero whole number, and compute such quotients. For example, create a story context for <math>(1/3) \div 4</math>, and use a visual fraction model to show the quotient. Use the relationship between multiplication and division to explain that <math>(1/3) \div 4 = 1/12</math> because <math>(1/12) \times 4 = 1/3</math>.</p> <p>b. Interpret division of a whole number by a unit fraction, and compute such quotients. For example, create a story context for <math>4 \div (1/5)</math>, and use a visual fraction model to show the quotient. Use the relationship between multiplication and division to explain that <math>4 \div (1/5) = 20</math> because <math>20 \times (1/5) = 4</math>.</p> <p>c. Solve real world problems involving division of unit fractions by non-zero whole numbers and division of whole numbers by unit fractions, e.g., by using visual fraction models and equations to represent the problem. For example, how much chocolate will each person get if 3 people share <math>1/2</math> lb of chocolate equally? How many <math>1/3</math>-cup servings are in 2 cups of raisins?</p>	<p>EDM 5.2 – Mixed Numbers</p>	<p>MJ1 (124)</p>
	<p>EDM 8.12 – Fraction Division</p>	<p>MJ2 (288, 289)</p>

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### Unit 2: Ratios – (5 Weeks)

**DESCRIPTION:**

Students will use their understanding of and skill with multiplication, division and fractions as they study ratios, rates and proportional relationships by viewing equivalent ratios and rates as derivations or extensions of pairs of rows (or columns) in the multiplication table, and by analyzing simple drawings that indicate the relative size of quantities. Students use a range of reasoning and representations to analyze proportional relationships. Their work in this unit will link with work in representing relationships between independent and dependent variables as well as setting the foundation for 8<sup>th</sup> grade work with linear equations. The Mathematical Practices should be evident throughout instruction and connected to the content addressed in this unit. Students should engage in mathematical tasks that provide an opportunity to connect content and practices.

Standards	Impact Lessons & Other Resources Available	Pages	
<p>The standards and resources listed below are <b>not</b> intentionally sequenced and should <b>not</b> be taught consecutively. To teach the concepts represented in this unit, teacher teams could use this unit overview and other available resources to craft a coherent and focused sequence of instruction that fully addresses the standards and description of this unit.</p>			
6.RP.1 Understand the concept of a ratio and use ratio language to describe a ratio relationship between two quantities. For example, “The ratio of wings to beaks in the bird house at the zoo was 2:1, because for every 2 wings there was 1 beak.” “For every vote candidate A received, candidate C received nearly three votes.”	Impact Lesson 5.1 – Ratios and Rates	290-307	
6.RP.2 Understand the concept of a unit rate $a/b$ associated with a ratio $a:b$ with $b \neq 0$ , and use rate language in the context of a ratio relationship. For example, “This recipe has a ratio of 3 cups of flour to 4 cups of sugar, so there is $3/4$ cup of flour for each cup of sugar.” “We paid \$75 for 15 hamburgers, which is a rate of \$5 per hamburger.” (Expectations for unit rates in this grade are limited to non-complex fractions).	Impact Lesson 5.1 – Ratios and Rates	290-307	
6.RP.3 Use ratio and rate reasoning to solve real-world and mathematical problems, e.g., by reasoning about tables of equivalent ratios, tape diagrams, double number line diagrams, or equations.	Impact Lesson 5.1 – Ratios and Rates	290-307	
	a. Make tables of equivalent ratios relating quantities with whole- number measurements, find missing values in the tables, and plot the pairs of values on the coordinate plane. Use tables to compare ratios.	Impact Lesson 6.1 – Use Percents	349-354 # 1- 21
	b. Solve unit rate problems including those involving unit pricing and constant speed. For example, if it took 7 hours to mow 4 lawns, then at that rate, how many lawns could be mowed in 35 hours? At what rate were lawns being mowed?	Impact Lesson 6.2 – A Percent of a Quantity	37-40
	c. Find a percent of a quantity as a rate per 100 (e.g., 30% of a quantity means $30/100$ times the quantity); solve problems involving finding the whole, given a part and the percent.	Impact Lesson 6.3 – Percents and Wholes	368-379, 384-387, parts of 390-392
	d. Use ratio reasoning to convert measurement.	Impact Lesson 7.4 - Capacity	450-461

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### Unit 3: Introduction to Rational Numbers<sup>1</sup> – (4 Weeks)

**DESCRIPTION:**

Students will extend their previous understanding of a number and the ordering of numbers to the full system of rational numbers, which includes negative rational numbers, and in particular negative integers. They reason about the order and absolute value of rational numbers and about the location of points in all four quadrants of the coordinate plane. The Mathematical Practices should be evident throughout instruction and connected to the content addressed in this unit. Students should engage in mathematical tasks that provide an opportunity to connect content and practices.

Standards	Impact Lessons & Other Resources Available	Pages
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<p>6.NS.5 Understand that positive and negative numbers are used together to describe quantities having opposite directions or values (e.g., temperature above/below zero, elevation above/below sea level, credits/debits, positive/negative electric charge); use positive and negative numbers to represent quantities in real-world contexts, explaining the meaning of 0 in each situation.</p>	<p>Impact Lesson 8.3 – Graph in Four Quadrants</p>	<p>509-514</p>
<p>6.NS.6 Understand a rational number as a point on the number line. Extend number line diagrams and coordinate axes familiar from previous grades to represent points on the line and in the plane with negative number coordinates.</p> <p>a. Recognize opposite signed of numbers as indicating locations on opposite sides of 0 on the number line; recognize that the opposite of the opposite of a number is the number itself, e.g., <math>-(-3) = 3</math>, and that 0 is its own opposite.</p> <p>b. Understand signs of numbers in ordered pairs as indicating locations in quadrants of the coordinate plane; recognize that when two ordered pairs differ only by signs, the location of the points are related by reflections across one or both axes.</p> <p>c. Find and position integers and other rational numbers on a horizontal or vertical number line diagram; find and position pairs of integers and other rational numbers on a coordinate plane.</p>	<p>Impact Lesson 8.3 – Graph in Four Quadrants</p>	<p>510-526</p>
<p>6.NS.7 Understand ordering and absolute value of rational numbers.</p> <p>a. Interpret statements of inequality as statements about the relative position of two numbers on a number line diagram. For example, interpret <math>-3 &gt; -7</math> as a statement that <math>-3</math> is located to the right of <math>-7</math> on a number line oriented from left to right.</p> <p>b. Write, interpret, and explain statements of order for rational numbers in real-world contexts. For example, write <math>-30^{\circ}\text{C} &gt; -70^{\circ}\text{C}</math> to express the fact that <math>-30^{\circ}\text{C}</math> is</p>	<p>Impact Lesson 6.1 – Use Percents</p>	<p>354-361 # 22-36, 41 - 43</p>

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<p>warmer than <math>-70^{\circ}\text{C}</math>.</p> <p>c. Understand the absolute value of a rational number as its distance from 0 on the number line; interpret absolute value as magnitude for a positive or negative quantity in a real-world situation. For example, for an account balance of <math>-30</math> dollars, write <math> -30  = 30</math> to describe the size of the debt in dollars.</p> <p>d. Distinguish comparisons of absolute value from statements about order. For example, recognize that an account balance less than <math>-30</math> dollars represents a debt greater than 30 dollars.</p>	<p>Impact Lesson 8.3 – Graph in 4 Quadrants</p>	<p>509-527</p>
<p>6.NS.8 Solve real-world and mathematical problems by graphing points in all four quadrants of the coordinate plane. Include use of coordinates and absolute value to find distances between points with the same first coordinate or the same second coordinate.</p>	<p>Impact Lesson 8.2 – Draw and Label Graphs</p>	<p>488-508</p>
	<p>Impact Lesson 8.3 – Graph in 4 Quadrants</p>	<p>509-527</p>

<sup>1</sup> *Work in this unit must not be limited to integers. Students should be working with positive and negative fractions and decimals as well as whole numbers.*

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### Unit 4: Expressions – (5 Weeks)

**DESCRIPTION:** Students will understand the use of variables in mathematical expressions. They will write expressions that correspond to given situations, evaluate expressions, and use expressions to solve problems. Students will understand that expressions in different forms can be equivalent, and they will use the properties of operations to rewrite expressions in equivalent forms. The Mathematical Practices should be evident throughout instruction and connected to the content addressed in this unit. Students should engage in mathematical tasks that provide an opportunity to connect content and practices.

Standards	Impact Lessons & Other Resources Available	Pages
The standards and resources listed below are <b>not</b> intentionally sequenced and should <b>not</b> be taught consecutively. To teach the concepts represented in this unit, teacher teams could use this unit overview and other available resources to craft a coherent and focused sequence of instruction that fully addresses the standards and description of this unit.		
6.EE.1 Write and evaluate numerical expressions involving whole-number exponents.	Impact Lesson 3.1 – Number Sense	113-116, 131-132, 117 # 3-16, 118-119 #21-23
6.EE.2 Write, read, and evaluate expressions in which letters stand for numbers. a. Write expressions that record operations with numbers and with letters standing for numbers. For example, express the calculation “Subtract $y$ from 5” as $5 - y$ . b. Identify parts of an expression using mathematical terms (sum, term, product, factor, quotient, coefficient); view one or more parts of an expression as a single entity. For example, describe the expression $2(8 + 7)$ as a product of two factors; view $(8 + 7)$ as both a single entity and a sum of two terms. c. Evaluate expressions at specific values of their variables. Include expressions that arise from formulas used in real-world problems. Perform arithmetic operations, including those involving whole- number exponents, in the conventional order when there are no parentheses to specify a particular order (Order of Operations). For example, use the formulas $V = s^3$ and $A = 6s^2$ to find the volume and surface area of a cube with sides of length $s = 1/2$ .	Impact Lesson 3.2 - Patterns	126-132
	Impact Lesson 3.2 - Patterns	136-137 # 9-31, 140 # 48-50,
	Impact Lesson 3.3 – Variables and Rules	143-173
6.EE.3 Apply the properties of operations to generate equivalent expressions. For example, apply the distributive property to the expression $3(2 + x)$ to produce the equivalent expression $6 + 3x$ ; apply the distributive property to the expression $24x + 18y$ to produce the equivalent expression $6(4x + 3y)$ ; apply properties of operations to $y + y + y$ to produce the equivalent expression $3y$ .	Impact Lesson 3.3 – Variables and Rules	143-173
	Impact Lesson 3.4 – Apply Properties	175-195
	Impact Lesson 9.2 - Backtracking	546-559
	Impact Lesson 9.3 – Guess-Check-and Improve	560-572
6.EE.4 Identify when two expressions are equivalent (i.e., when the two expressions name the same number regardless of which value is substituted into them). For example, the expressions $y + y + y$ and $3y$ are equivalent because they name the same number regardless of which number $y$ stands for.	Impact Lesson 3.3 – Variables and Rules	143-173

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### Unit 5: Equations – (5 Weeks)

**DESCRIPTION:**

Students will write equations that correspond to given situations and use formulas to solve problems. Students will learn that solutions of an equation are the values of the variables that make the equation true. Students will use properties of operations and the idea of maintaining the equality of both sides of an equation to solve simple one-step equations. Students will also construct and analyze tables, such as quantities that are in equivalent ratios, and use equations to describe relationships between quantities. The Mathematical Practices should be evident throughout instruction and connected to the content addressed in this unit. Students should engage in mathematical tasks that provide an opportunity to connect content and practices.

Standards	Impact Lessons & Other Resources Available	Pages
The standards and resources listed below are <b>not</b> intentionally sequenced and should <b>not</b> be taught consecutively. To teach the concepts represented in this unit, teacher teams could use this unit overview and other available resources to craft a coherent and focused sequence of instruction that fully addresses the standards and description of this unit.		
6.EE.5 Understand solving an equation or inequality as a process of answering a question: which values from a specified set, if any, make the equation or inequality true? Use substitution to determine whether a given number in a specified set makes an equation or inequality true.	Impact Lesson 9.1 – Understand Equations	534-545
	Impact Lesson 9.2 - Backtracking	546-559
	Impact Lesson 9.3 – Guess-Check-and-Improve	572
6.EE.9 Use variables to represent two quantities in a real-world problem that change in relationship to one another; write an equation to express one quantity, thought of as the dependent variable, in terms of the other quantity, thought of as the independent variable. Analyze the relationship between the dependent and independent variables using graphs and tables, and relate these to the equation. For example, in a problem involving motion at constant speed, list and graph ordered pairs of distances and times, and write the equation $d = 65t$ to represent the relationship between distance and time.	Impact Lesson 3.2 – Patterns	133-135, 137 # 32-35, 139 # 40, 141 # 52, 142 # 55
	Impact Lesson 3.3 – Variables and Rules	143-173
	Impact Lesson 8.1 – Interpret Graphs	468- 488
	Impact Lesson 8.2 – Draw and Label Graphs	489-508
6.EE.6 Use variables to represent numbers and write expressions when solving a real-world or mathematical problem; understand that a variable can represent an unknown number, or, depending on the purpose at hand, any number in a specified set.	Impact Lesson 3.3 – Variables and Rules	143-173
	Impact Lesson 9.1 – Understand Equations	534-545
	Impact Lesson 9.2 – Backtracking	546-559
	Impact Lesson 9.3 – Guess-Check-and-Improve	560-572
6.EE.7 Solve real-world and mathematical problems by writing and solving equations of the form $x + p = q$ and $px = q$ for cases in which $p$ , $q$ and $x$ are all nonnegative rational numbers.	Impact Lesson 3.3 - Variables and Rules	143-173
	Impact Lesson 9.1 – Understand Equations	534-545
	Impact Lesson 9.2 – Backtracking	546-559
	Impact Lesson 9.3 – Guess-Check-and-Improve	560-572

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6.EE.8 Write an inequality of the form $x > c$ or $x < c$ to represent a constraint or condition in a real-world or mathematical problem. Recognize that inequalities of the form $x > c$ or $x < c$ have infinitely many solutions; represent solutions of such inequalities on number line diagrams.	Impact Lesson 9.1 – Understanding Equations	534-545
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### Unit 6: Concepts in Geometry – (1 Week)

**DESCRIPTION:**

Students in grade 6 build on their work with area in elementary school by reasoning about relationships among shapes to determine area, surface area, and volume. They will find areas of right triangles, other triangles, and special quadrilaterals by decomposing these shapes, rearranging or removing pieces, and relating the shapes to rectangles. Using these models, students will discuss, develop, and justify formulas for areas of triangles and parallelograms. Students will find areas of polygons and surface areas of prisms and pyramids by decomposing them into pieces whose area they can determine. They will reason about right rectangular prisms with fractional side lengths to extend formulas for the volume of a right rectangular prism to fractional side lengths. They will prepare for work on scale drawings and constructions in grade 7 by drawing polygons in the coordinate plane. The Mathematical Practices should be evident throughout instruction and connected to the content addressed in this unit. Students should engage in mathematical tasks that provide an opportunity to connect content and practices.

Standards	Impact Lessons & Other Resources Available	Pages
The standards and resources listed below are <b>not</b> intentionally sequenced and should <b>not</b> be taught consecutively. To teach the concepts represented in this unit, teacher teams could use this unit overview and other available resources to craft a coherent and focused sequence of instruction that fully addresses the standards and description of this unit.		
6.G.1 Find the area of right triangles, other triangles, special quadrilaterals, and polygons by composing into rectangles or decomposing into triangles and other shapes; apply these techniques in the context of solving real-world and mathematical problems.	Impact Lesson 7.1 – Squares	398-419
	Impact Lesson 7.2 – Calculate Areas	425-433 # 1-10, 15-20, 25-31, 35, 36
6.G.3 Draw polygons in the coordinate plane given coordinates for the vertices; use coordinates to find the length of a side joining points with the same first coordinate or the same second coordinate. Apply these techniques in the context of solving real-world and mathematical problems.	Impact Lesson 8.3 – Graph in Four Quadrants	520-521
6.G.4 Represent three-dimensional figures using nets made up of rectangles and triangles, and use the nets to find the surface area of these figures. Apply these techniques in the context of solving real-world and mathematical problems.	Impact Lesson 7.3 – Surface Area and Volume	434-448

**Bridge Guidance:**

Standards	Impact Lessons & Other Resources Available	Pages
5.MD.3 Recognize volume as an attribute of solid figures and understand concepts of volume measurement. a. A cube with side length 1 unit, called a “unit cube,” is said to have “one cubic unit” of volume, and can be used to measure volume. b. A solid figure which can be packed without gaps or overlaps using n unit cubes is said to have a volume of n cubic units.	EDM 9.8 – Volume of Rectangular Prisms	MJ2 (321, 322), MM ( 279)
	EDM 9.10 – Capacity: Liter, Milliliter, And cubic Centimeter	MJ2 (327-329)
	EDM 11.4 – Volume Of Pyramids And Cones	SRB (137), MM (330)
5.MD.4 Measure volumes by counting unit cubes, using cubic cm, cubic in, cubic ft, and improvised units.	EDM 9.8 – Volume of Rectangular Prisms	MJ2 (322), MM (279)
	EDM 11.5 – Finding Volume By A Displacement Method	MJ2 (300, 301), MM (331, 332)

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<p>5.MD.5 Relate volume to the operations of multiplication and addition and solve real world and mathematical problems involving volume.</p>	<p>EDM 9.8 – Volume of Rectangular Prisms</p>	<p>MJ2 (322), MM (279)</p>
<p>a. Find the volume of a right rectangular prism with whole-number side lengths by packing it with unit cubes, and show that the volume is the same as would be found by multiplying the edge lengths, equivalently by multiplying the height by the area of the base. Represent threefold whole-number products as volumes, e.g., to represent the associative property of multiplication.</p> <p>b. Apply the formulas <math>V=l \times w \times h</math> and <math>V=b \times h</math> for rectangular prisms to find volumes of right rectangular prisms with whole- number edge lengths in the context of solving real world and mathematical problems.</p> <p>c. Recognize volume as additive. Find volumes of solid figures composed of two non-overlapping right rectangular prisms by adding the volumes of the non-overlapping parts, applying this technique to solve real world problems.</p>	<p>EDM 9.10 – Capacity: Liter, Milliliter, And Cubic Centimeter</p>	<p>MJ2 (327-329)</p>

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### Unit 7: Introduction to Statistics – (2 Weeks)

**DESCRIPTION:**

Building on and reinforcing their understanding of number, students begin to develop their ability to think statistically. Students will recognize that a data distribution may not have a definite center and that different ways to measure center yield different values. The median measures center in the sense that it is roughly the middle value. The mean measures the center in the sense that it is the value that each data point would take on if the total of the data values were redistributed equally, and also in the sense that it is a balance point. Students will recognize that a measure of variability (interquartile range or mean absolute deviation) can also be useful for summarizing data because two very different sets of data can have the same mean and median, yet be distinguished by their variability. Students will learn to describe and summarize numerical data sets, identifying clusters, peaks, gaps, and symmetry considering the context in which the data were collected. The Mathematical Practices should be evident throughout instruction and connected to the content addressed in this unit. Students should engage in mathematical tasks that provide an opportunity to connect content and practices.

Standards	Impact Lessons & Other Resources Available	Pages
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6.SP.1 Recognize a statistical question as one that anticipates variability in the data related to the question and accounts for it in the answers. For example, “How old am I?” is not a statistical question, but “How old are the students in my school?” is a statistical question because one anticipates variability in students’ ages.	Impact Lesson 4.4 – What is Typical?	265-281
6.SP.2 Understand that a set of data collected to answer a statistical question has a distribution which can be described by its center, spread, and overall shape.	Impact Lesson 4.4 – What is Typical?	265-281
6.SP.3 Recognize that a measure of center for a numerical data set summarizes all of its values with a single number, while a measure of variation describes how its values vary with a single number.	Impact Lesson 4.4 – What is Typical?	265-281
6.SP.4 Display numerical data in plots on a number line, including dot plots, histograms, and box plots.	Impact Lesson 4.4 – What is Typical?	265-281
	Impact Lesson 8.1 – Interpret Graphs	468- 487
	Impact Lesson 10.1 – Data Displays	578-580
	Impact Lesson 10.2 – Collect and Analyze Data	585-587, parts of 592-600
6.SP.5 Summarize numerical data sets in relation to their context, such as by: <ul style="list-style-type: none"> <li>a. Reporting the number of observations.</li> <li>b. Describing the nature of the attribute under investigation, including how it was measured and its units of measurement.</li> <li>c. Giving quantitative measures of center (median and/or</li> </ul>	Impact Lesson 4.4 – What is Typical?	265-281

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<p>mean) and variability (interquartile range and/or mean absolute deviation), as well as describing any overall pattern and any striking deviations from the overall pattern with reference to the context in which the data were gathered.</p> <p>d. Relating the choice of measures of center and variability to the shape of the data distribution and the context in which the data were gathered.</p>	Impact Lesson 10.2 – Collect and Analyze Data	601-616
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